



# Precalculus

## Topic: Complex Numbers

### Instructions

Solve the following problems related to complex numbers. Show all work clearly and check your solutions.

## Practice Problems

1. Find the real and imaginary parts of the following complex numbers.

(i) $4 - 7i$	(v) $i\sqrt{3}$
(ii) $\frac{-3+5i}{2}$	(vi) $\sqrt{3} + \sqrt{-4}$
(iii) $\frac{6-5i}{3}$	(vii) $\frac{5+3i}{2}$
(iv) $8 + 7i$	(viii) $-\frac{1}{2}$

2. Evaluate the expression and write the result in the form  $a + bi$ .

(i) $(3 + 4i) + (5 - 2i)$	(vi) $(2i)^4$
(ii) $(7 - i)(4 + 2i)$	(vii) $(6 + 5i)(2 - 3i)$
(iii) $(1 - 3i) + (2 + 6i)$	(viii) $\frac{1}{1+i} - \frac{1}{1-i}$
(iv) $\frac{2-3i}{1-2i}$	(ix) $(1 - 2i) + (3 + 4i)$
(v) $(3 + 2i) - (5 - 6i)$	(x) $\frac{(1+2i)(3-i)}{2+i}$

3. Evaluate the following radical expressions and express the result in the form  $a + bi$ .

$$(i) \sqrt{-25}$$

$$(v) \quad \sqrt{16} + \sqrt{-9}$$

$$(ii) \sqrt{\frac{-9}{4}}$$

$$(vi) \frac{2+\sqrt{-8}}{1+\sqrt{-2}}$$

$$(iii) \sqrt{-3} \cdot \sqrt{-12}$$

$$(iv) \quad (3 - \sqrt{-5})(1 + \sqrt{-1})$$

(vii)  $\sqrt{-49}$

4. Find all solutions of the equation and express them in the form  $a + bi$ :

$$(i) \ x^2 + 49 = 0$$

$$(vi) \ x^2 - 3x + 3 = 0$$

$$(ii) \ x^2 - 4x + 5 = 0$$

$$(vii) \ z + 3 + \frac{3}{z} = 0$$

$$(iii) \ x^2 + 2x + 5 = 0$$

$$(v_H) \approx +\infty + z^{-\alpha}$$

$$(iv) \quad x^2 + x + 1 = 0$$

(viii)  $6x^2 + 12x + 7 =$

## Multiple-Choice Questions

1. What is the result when  $6 + 3i$  is subtracted from  $2 - 5i$ ?

- A.  $-4 - 8i$       C.  $-4 + 8i$   
 B.  $8 + 8i$       D.  $4 - 8i$

2. What is the result when  $2 + 5i$  is added to  $3 - 4i$ ?

- A.  $5 + i$       C.  $1 + i$   
B.  $5 + 9i$       D.  $5 + 9i$

3. What is the result of dividing  $(3 + 2i)$  by  $1 + 4i$ ?

- A.  $\frac{3+2i}{1+4i}$       C.  $1+i$   
B.  $\frac{10+11i}{17}$       D.  $2-4i$

4. What is the result of  $\sqrt{-16}$ ?

- A.  $4i$       C. 4  
B.  $-4i$       D.  $-4$

5. What is the solution to the equation  $2x^2 + 3x + 5 = 0$ ?

- A.  $x = \frac{-3 \pm \sqrt{9-40}}{4}$

B.  $x = -\frac{3 \pm \sqrt{9-20}}{4}$

C.  $x = \frac{-3 \pm \sqrt{16}}{4}$

D.  $x = \frac{-5 \pm \sqrt{16}}{4}$