

# A Level Maths

### **Topic:** Transformations of Graphs

#### Instructions

Answer all questions. Show complete working. Apply appropriate transformations to graphs based on the given functions.

### **Practice Questions**

- 1. Given the function  $f(x) = x^2$ , write the equation for the following transformations:
  - (i) Shift  $f(x) = x^2$  3 units to the right.
  - (ii) Reflect  $f(x) = x^2$  in the x-axis.
  - (iii) Stretch  $f(x) = x^2$  vertically by a factor of 2.
  - (iv) Translate  $f(x) = x^2 4$  units up.
- 2. The graph of  $y = \sqrt{x}$  is shifted 5 units to the left and 2 units down. Write the equation of the transformed graph.
- 3. Consider the function g(x) = 3x 1. Apply the following transformations and write the equations of the transformed graphs:
  - (i) Translate 4 units up.
  - (ii) Reflect in the y-axis.
  - (iii) Stretch vertically by a factor of 2.
- 4. Given the function  $h(x) = \sin x$ , write the equation of the transformed graph when it is:
  - (i) Reflected in the x-axis.
  - (ii) Shifted 90 units to the right.
  - (iii) Stretched vertically by a factor of 3.

- 5. For the function  $y = \cos x$ , perform the following transformations and write the equation for each:
  - (i) Translate 2 units to the left.
  - (ii) Reflect in the y-axis.
  - (iii) Compress vertically by a factor of 1/2.
- 6. Consider the function y = |x 1|. Apply the following transformations and write the equations for the transformed graphs:
  - (i) Translate 3 units to the right.
  - (ii) Reflect in the x-axis.
  - (iii) Stretch horizontally by a factor of 2.
- 7. Given the function  $f(x) = x^3$ , write the equations for the following transformations:
  - (i) Reflect  $f(x) = x^3$  in the y-axis.
  - (ii) Translate  $f(x) = x^3$  5 units to the left.
  - (iii) Stretch  $f(x) = x^3$  vertically by a factor of 4.
- 8. Consider the function  $y = e^x$ . Apply the following transformations:
  - (i) Translate 3 units to the left.
  - (ii) Stretch vertically by a factor of 2.
  - (iii) Reflect in the x-axis.

## **Multiple-Choice Questions**

1. The transformation of the graph of  $y=x^2$  that results in a vertical stretch by a factor of 3 is:

A. 
$$y = 3x^2$$

B. 
$$y = x^2 + 3$$

C. 
$$y = 3(x^2)$$

D. 
$$y = x^2 - 3$$

2. The graph of y = |x| is reflected in the x-axis. The equation of the new graph is:

$$A. y = -|x|$$

B. 
$$y = |x|$$

C. 
$$y = x$$

D. 
$$y = -x$$

3. If the graph of  $y=x^2$  is shifted 3 units to the left, the equation of the transformed graph is:

A. 
$$y = (x+3)^2$$

B. 
$$y = (x - 3)^2$$

C. 
$$y = x^2 + 3$$

D. 
$$y = x^2 - 3$$

4. For the function  $y = \cos x$ , if the graph is stretched vertically by a factor of 2, the new equation will be:

A. 
$$y = 2\cos x$$

B. 
$$y = \cos 2x$$

C. 
$$y = 2x$$

$$D. y = \cos x + 2$$

5. The equation y=|x+2| is reflected in the y-axis. The equation of the transformed graph is:

A. 
$$y = |x - 2|$$

B. 
$$y = |x + 2|$$

C. 
$$y = |-x + 2|$$

D. 
$$y = |x - 2|$$

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